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EXERCISE BOOK CAHIER D'EXERCICES

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SUBJECT/SUJET ELEC 315

Lecture 0

9/03/19

LEC

Course Overview:

1 midterm \rightarrow 25%

2 Final \rightarrow 50%

Assignments throughout \rightarrow 15%

Participation (Iclicker) \rightarrow 10%

Japan Solar Workshop \rightarrow 10-3:00pm Kaiser

Office hours:

Tuesday \rightarrow 11:00 - 12:00

4:00 - 5:00

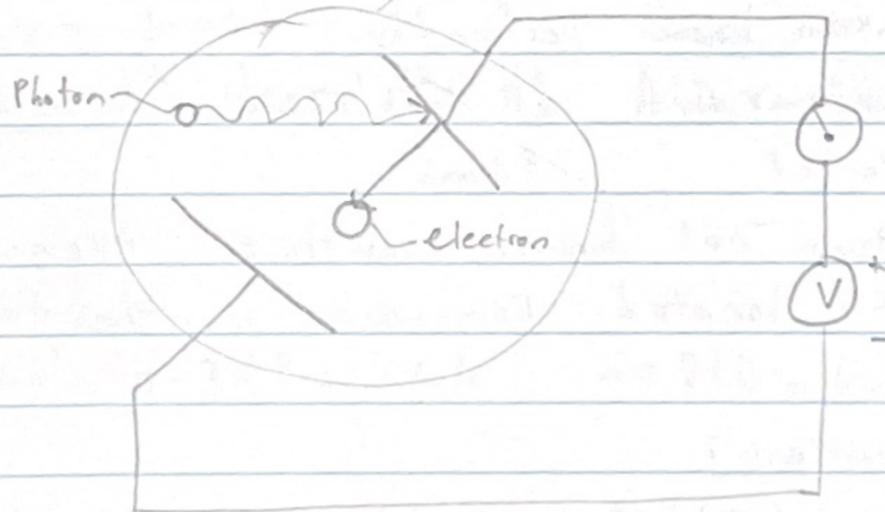
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Lecture 1

Photoelectric effect:

vacuum (e^- 's don't travel far in air)



Conservation of energy: energy of incoming photon = energy for electron to get out

$$KE_{\text{Max}} = -e \cdot \theta + h\nu$$

Plank's constant
Frequency

+
Kinetic energy
for the electron

Photons:

$$\text{Energy} = h\nu$$

$$\text{(Momentum)} \quad p = \frac{h}{\lambda}$$

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Lecture 2

Conservation of energy: (assuming perfect collision)

$$\text{Photon (energy)} = \text{work function} + \text{kinetic energy}$$

- we use voltage to slow down approaching electrons

$$\therefore \text{Photon (energy)} = \text{work function} + \text{applied voltage}$$

(at the point where current cuts off)

Heisenberg Uncertainty Principle:

① Perfect sinusoid

• momentum known perfectly

• $(-\infty, \infty)$ can't be localized to a point/region

② Wave packet

• momentum not known (multiple frequencies)

• $(-x, x)$ located somewhere in the region x

Basic Equations:

① $E = h\nu$ (ν) Frequency
(h) Planck's constant

② $\lambda = \frac{h}{p}$

$$\sin(kx - \omega t) \quad | \quad k = \frac{2\pi}{\lambda} \quad | \quad \omega = 2\pi f \quad | \quad v = \lambda f$$

Kinetic energy:

$$KE = \frac{p^2}{2m} \quad | \quad KE = \frac{h^2}{2m\lambda^2} \quad | \quad KE = \frac{-\hbar^2}{2m} \cdot \frac{d^2\psi}{dx^2}$$

Schrödinger Equation:

$$i \cdot \hbar \cdot \frac{d\psi}{dt} = \frac{-\hbar^2}{2m} \cdot \frac{d^2\psi}{dx^2} + U \cdot \psi$$

$$E(n) = \frac{n^2 \pi^2 \hbar^2}{2mL^2}$$

Lecture 3

$$\hbar = \frac{h}{2\pi}$$

(More confined \rightarrow more discrete)

1D Confinement: $E(n) = \frac{n^2 \pi^2 \hbar^2}{2mL^2}$

(less discrete energy levels)

2D Confinement: $E(n_x, n_y) = \frac{h^2}{8m} \left(\frac{n_x^2}{x_0^2} + \frac{n_y^2}{y_0^2} \right)$

Atomic Orbitals:

$n=1$ (s orbital) $n=2$ (p orbitals) $n=3$ (d orbitals)

(Degrees of degeneracy) = (# of wave functions @ specific energy level)

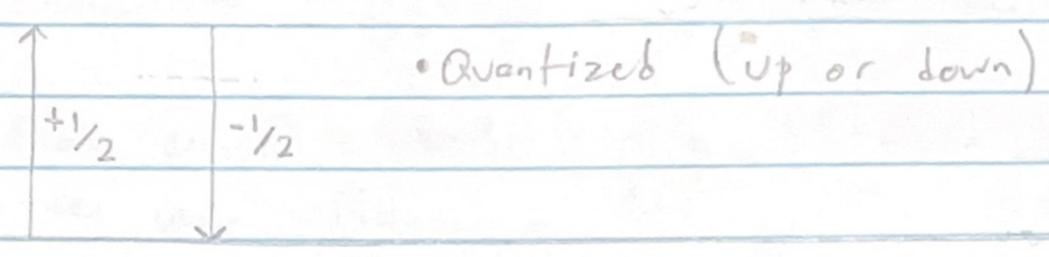
Lecture 4

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Covalent Bonding: (Bringing two H atoms close together)

- Energy levels split into new more levels
- Solid structure of many atoms can start to have a continuous looking number of energy levels (why solar cell can absorb anywhere)

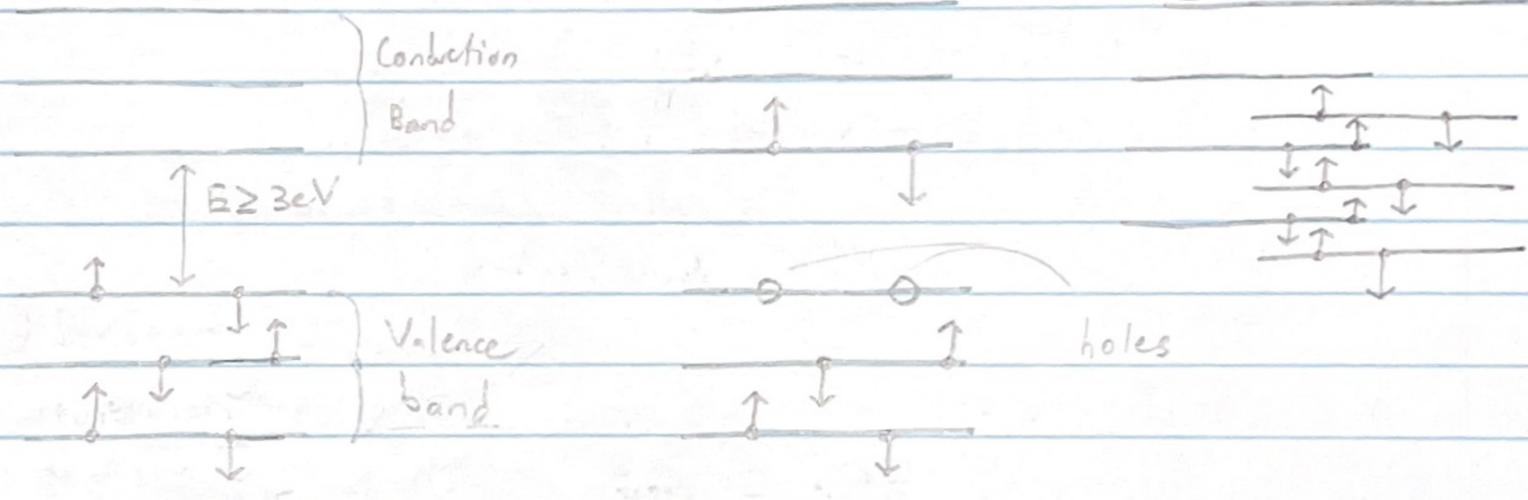
Electron Spin:



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Lecture 5 (solids and Semiconductors) SLIDE SET

Insulator: Semiconductor: Conductor (metal):



Q6 c-d (b-c-d) total energy = kinetic energy

Q8g Assume $n_x = n_y = n_z = 1$ (ground state) assume material is silicon

Polycrystalline:
Grain boundaries non-conductive

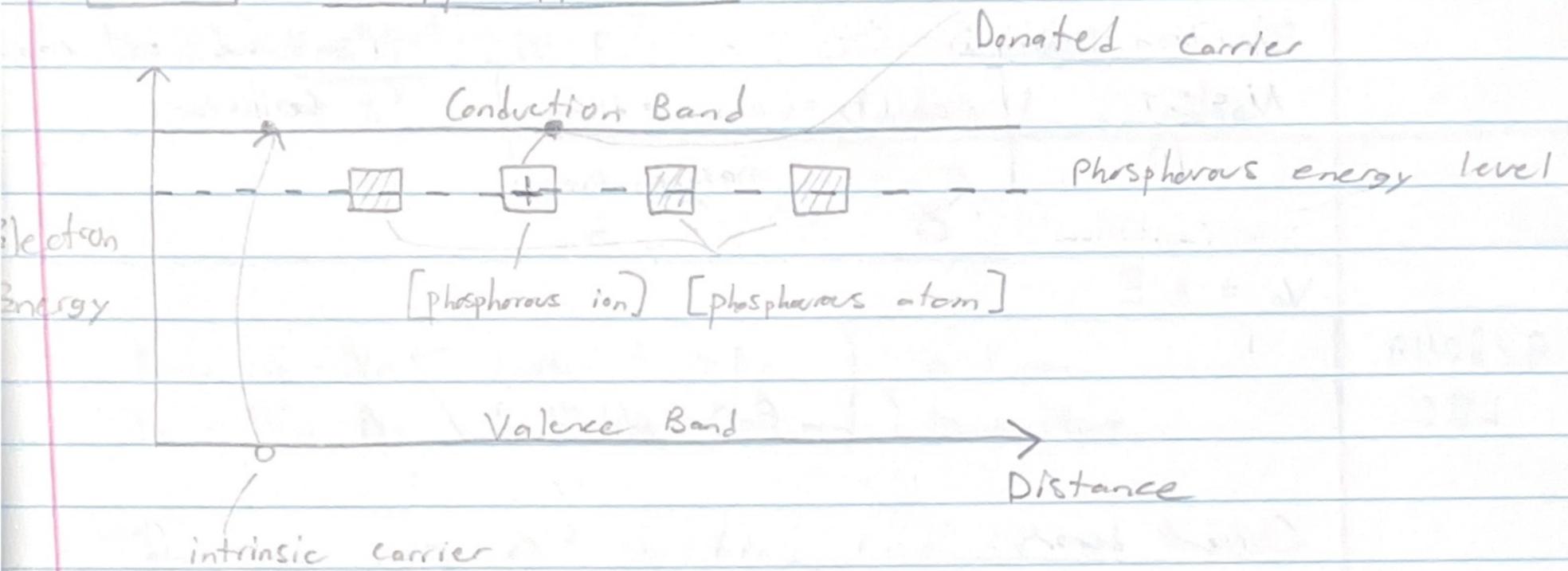
SS11 i subscript means intrinsic ie: undoped

$n_i = p_i \rightarrow$ # holes in valence band
 \hookrightarrow # e's in conduction band

Lecture 6

SS 15

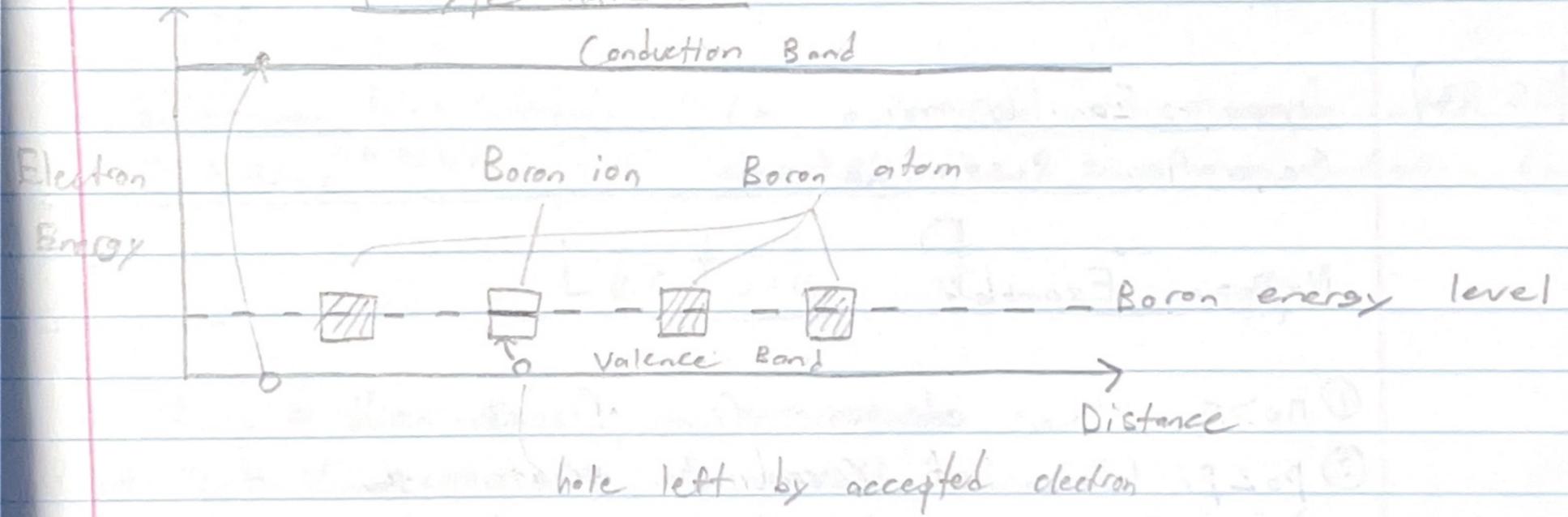
n-Type Material:



Electron effective mass:

$$m_0 = 9.1 \times 10^{-31} \text{ kg [Free electron mass]}$$

p-Type material:



Current:

$$J = \sigma E \text{ (Current density = Conductivity} \cdot \text{Electric field)}$$

What affects Conductivity:

- ① time between collisions
- ② electron mobility (effective mass)
- ③ # of carriers per unit volume

$$\text{Current} = \frac{L \cdot A \cdot n_0 \cdot q_e}{T} \quad \text{where: } \frac{L}{T} = v_e$$

Electron Mobility:

$$v = \frac{eE}{m}$$

$$\left[\text{mobility} = \frac{e_{\text{charge}} \cdot \text{time}}{\text{mass effective}} \right]$$

$T =$ time between collisions

$$v_e = \mu E$$

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Lecture 7

Current density:

$$J = eE(n_0 \mu_e + p_0 \mu_h)$$

Where: $n_0 =$ electron density in conduction band

$p_0 =$ hole density in valence band

$\mu_e =$ electron mobility

$\mu_h =$ hole mobility

SS 52

Dynamic Equilibrium:

Generation = Recombination

N-Doping Example:

① $n_0 > n_i$ (Donor electrons from Phosphorus)

② $p_0 < p_i$ (Rate of recombination greater than at intrinsic)

SS 60

Rate of Generation: [@ Equilibrium] $R = G$

$$G = f_g(\text{Temp})$$

Rate of Recombination:

$$R = f_r(\text{Temp}) n_0 p_0$$

$$n_0 p_0 = n_i^2$$

$$\therefore n_0 p_0 = n_i^2$$

Density of states: (3D) [how many states per unit volume at the given energy level (E)]

$$g_c(E) = \frac{(m_e^*)^{3/2}}{\pi^2 \hbar^3} \sqrt{2(E - E_c)}$$

Conduction band edge

Lecture 8

$$\begin{aligned} n_0 &= N_D - N_A && (\text{when } N_D > N_A) \\ p_0 &= N_A - N_D && (\text{when } N_A > N_D) \end{aligned} \quad \left. \begin{array}{l} \text{@ Room} \\ \text{temperature} \end{array} \right\}$$

Then, use $n_0 p_0 = n_i^2$ to find n_0, p_0

Counting electrons:

where:

n = total # e's in conduction band

$$n = \int_{CB} g_c(E) \cdot f(E) dE$$

$g_c(E)$ = Density of states

$f(E)$ = occupancy probability

Boltzmann Distribution:

$$f(e) \approx e^{-(E - E_F)/kT}$$

(Can only use this approximation above the Fermi level i.e.: conduction band)

Lecture 9

N_D = # donor atoms per unit volume

N_A = # acceptor atoms per unit volume

n-doped material:

$$n_0 = N_D \quad (\text{@ room temperature})$$

p-doped material:

$$p_0 = N_A \quad (\text{@ room temperature})$$

Counting holes:

$$P_0 = \int_{\text{Bottom VB}}^{\text{Top VB}} g_v(E)(1-f(E))dE$$

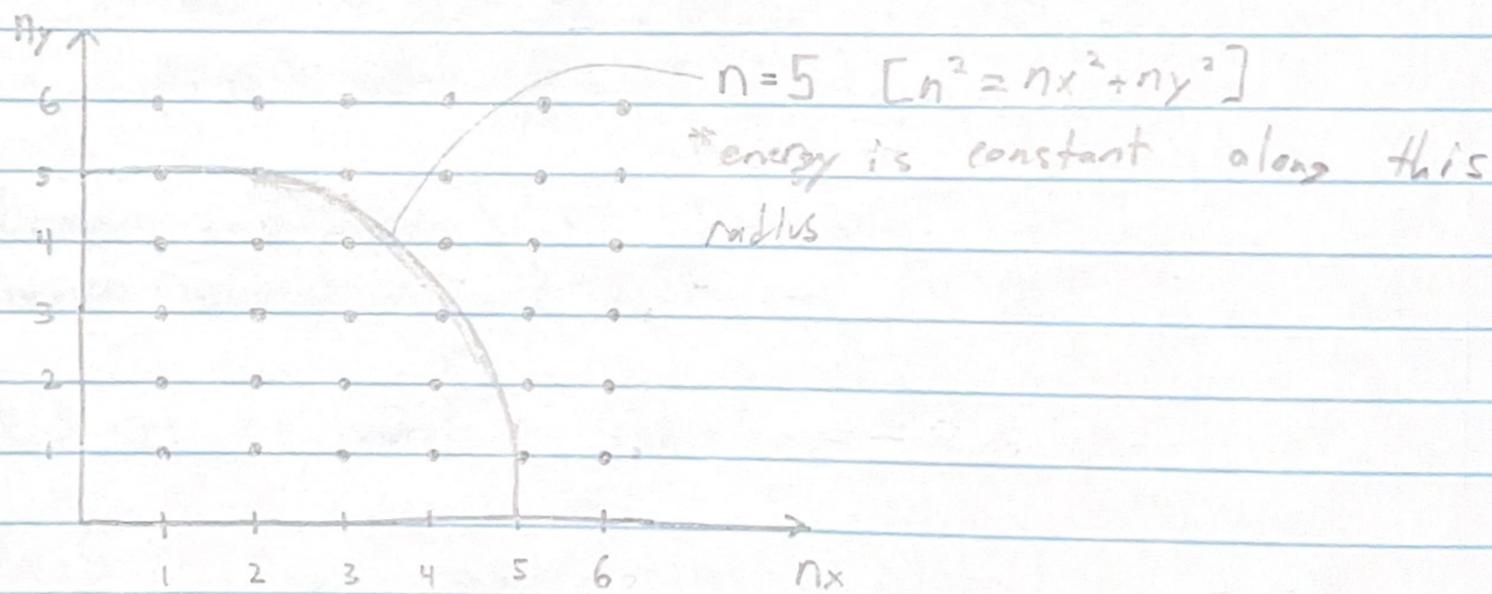
3D box:

$$E = \frac{h^2}{8m} \left[\frac{n_x^2}{L_x^2} + \frac{n_y^2}{L_y^2} + \frac{n_z^2}{L_z^2} \right]$$

2D box: if $(L_z \ll L_x \text{ and } L_y)$ and $(L_x = L_y)$

$$E_{2D} = \frac{h^2}{8mL_x^2} [n_x^2 + n_y^2]$$

Find density of States:



$$N = \frac{\pi n^2}{2}$$

Intrinsic e^- 's:

$$n_i^2 = 10^{20}$$

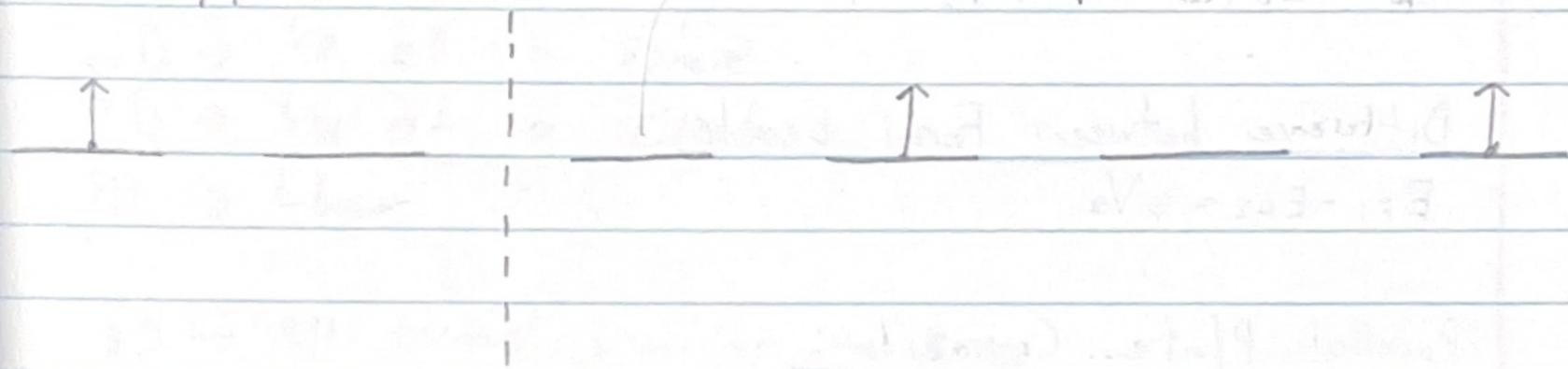
Lecture 10

Filling Level:

n

room for 2 e's

1 - P

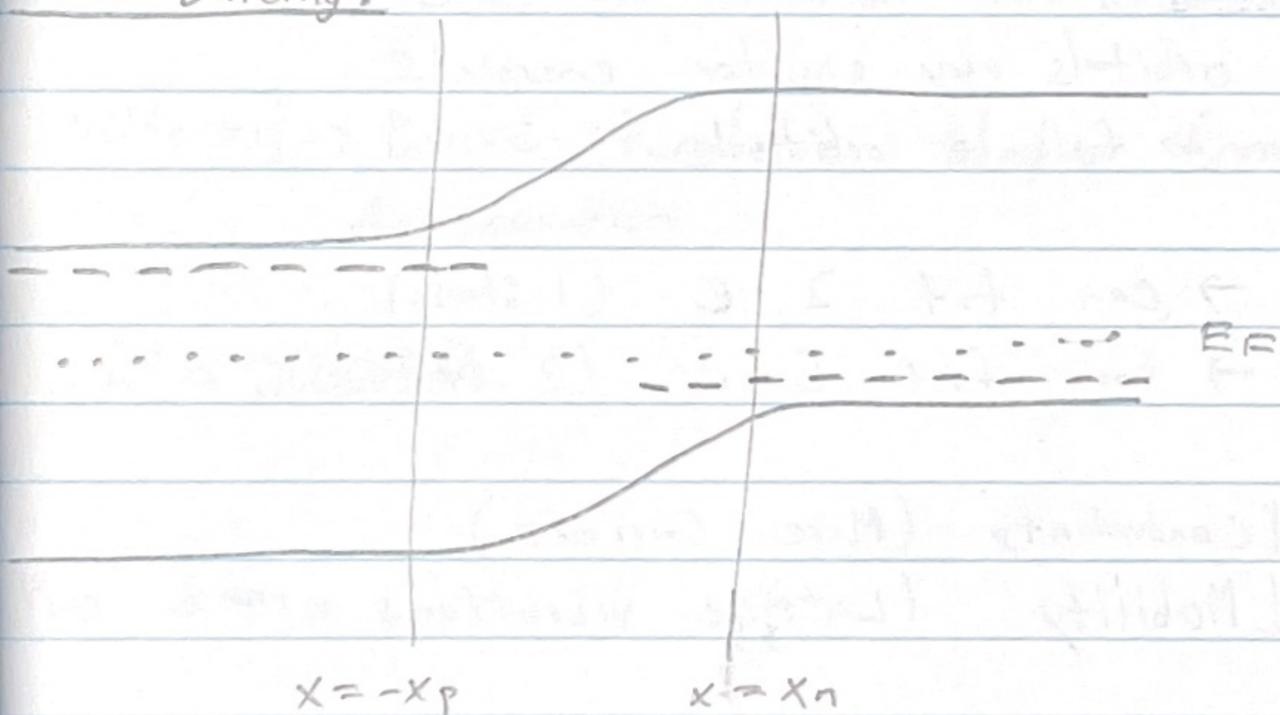


$$E_F = \frac{1}{4}$$

$$E_F = \frac{2}{8} = \frac{1}{4}$$

Lecture 11

Band Bending:



SS 173 $U(x) \propto \frac{+e\phi}{2\epsilon} x^2$

SS 179 ASN 3 Q3 Derivation

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Diode Equation:

$$I = I_0 (e^{eV_0/RT} - 1)$$

Difference between Fermi Levels:

$$E_{F1} - E_{F2} = eV_0$$

Parallel Plate Capacitor:

$$C = \frac{\epsilon_r \epsilon_0 A}{d}$$

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Lecture 13

Review Orbitals:

2s and 2p orbitals very similar energies

ie: Beryllium \rightarrow full p orbital

s orbital \rightarrow can fit 2 e (1 state)

p orbital \rightarrow can fit 6 e (3 states)

Intrinsic
Material

\uparrow Temp \rightarrow \uparrow Conductivity (More carriers)

\uparrow Temp \rightarrow \downarrow Mobility (Lattice vibrations = more collisions)

* But $n_i \gg N_c$

Doped
Material

\uparrow Temp \rightarrow \downarrow Conductivity

\uparrow Temp \rightarrow \downarrow Mobility

$N_0 \gg n_i$ so $n_0 = \text{Fixed}$ $\therefore N_c$ dominates

\uparrow Temp \rightarrow \uparrow Conductivity (Intrinsic Semiconductor)

\uparrow Temp \rightarrow \downarrow Conductivity (Metal)

\uparrow Temp \rightarrow \downarrow \rightarrow \uparrow Conductivity (Doped Semiconductor)

Midterm → Derive either 1D, 2D or 3D $g(E)$
on a midterm

3D → $\frac{1}{8}$ of a sphere

2D → $\frac{1}{4}$ of a circle

1D → Line

3D → All terms similar in size

2D → One term much bigger (ie: small L)

1D → Two terms much bigger (ie: small L 's)

Silicon Band Gap = 1.12eV

Midterm → One PN Junction Band Diagram (either eqn, Fwd, reverse)

Midterm → Derive Parabolic shape from depletion
Approximation

$$kT = 0.025V$$

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** Common Exam Question → SS. 24

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Lecture 15

Polarization:

$$P = P_0 e^{-t/\tau} \rightarrow P(\omega) = \frac{P_0}{\tau + j\omega}$$

Susceptibility:

$$X(\omega) = \frac{P(\omega)}{\epsilon_0 E_0} = \frac{X_0}{\tau + j\omega}$$

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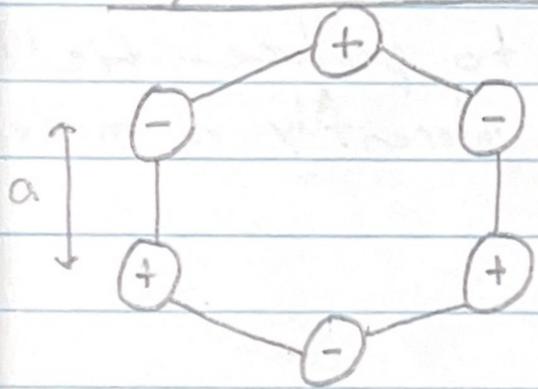
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$$\text{Energy} = \frac{1}{2} CV^2$$

$eE\lambda \geq E_g$ (For electron to be promoted)

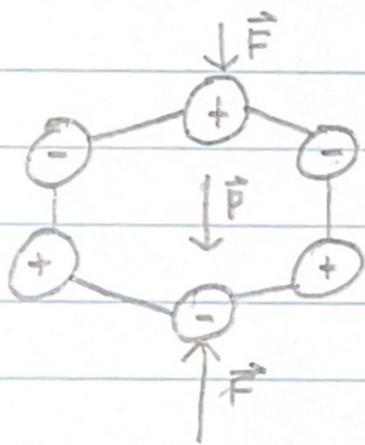
Lecture 16

Crystal Structure A:



- No dipole moment
- $P = 0$

Crystal Structure (B) [Compressed]:



- Net dipole moment
- \vec{P} is non-zero

Direct Piezoelectric Equation:

$$P_x = d_x T_x \quad \text{where:}$$

P_x = Polarization

T = applied stress \vec{F}/Area

d_x = piezoelectric constant

$$\frac{\Delta L}{L} = d E$$

$$E = \frac{\Delta L}{\Delta L}$$

$$\frac{E}{L} = \frac{\Delta L}{\Delta L^2}$$

$$V = \frac{\Delta L}{\Delta L}$$